

Maths for Computing

Assignment 6

1. (5 marks) Construct a DFA for $L = \{w \mid w \text{ contains equal number of occurrences of } 01 \text{ and } 10 \text{ as substring of } w\}$ over $\{0,1\}$. For instance, $010 \in L$, $0110 \in L$, $0111 \notin L$, $10110 \notin L$. Justify with a casual proof why the constructed DFA is deciding L .
2. (5 marks) Prove or disprove that $L = \{0^n \mid n \text{ is a perfect square}\}$ over $\{0,1\}$ is a regular language.
3. (5 marks) Construct a CFG for $L = \{a^i b^j c^k \mid i \neq j \text{ or } j \neq k, \text{ where } i, j, k \in \mathbb{Z}^+\}$ over $\{a, b, c\}$.